



1)

(1)  $x = \sqrt{3}$

(2)  $(x + 2)(x - 1) = x^2 - 2x - 3$

(3)  $7(3x + 4y)(3x - 4y)$

(4) 4

2)

(1)  $2y = 10 - y^2$

$\therefore y^2 + 2y - 10 = 0$

Comparing with  $ay^2 + by + c = 0$  [Here  $y = x$ ] we get,

$a = 1, b = 2, c = -10$

(2)  $7m^2 = 21m$

$\therefore 7m - 21m = 0$

$\therefore 7m(m - 3) = 0$

$\therefore 7m = 0$  or  $m - 3 = 0$

$\therefore m = \frac{0}{7}$  or  $m = 3$

$\therefore m = 0$  or  $m = 3$

$\therefore$  The roots of the given quadratic equation are 0 and 3.

3)

(1)  $\sqrt{5}x^2 - x - \sqrt{5} = 0$

Comparing with  $ax^2 + bx + c = 0$  we get,

$a = \sqrt{5}, b = -1, c = -\sqrt{5}$

$\Delta = b^2 - 4ac$

$= (-1)^2 - 4 \times \sqrt{5} \times -\sqrt{5}$

$= 1 + 20$

$\Delta = 21$

(2)  $2y^2 - 5y + 10 = 0$

Comparing with  $ay^2 + by + c = 0$  [Here  $y = x$ ] we get,

$a = 2, b = -5, c = 10$

$\Delta = b^2 - 4ac$

$= (-5)^2 - 4 \times 2 \times 10$

$= 25 - 80$

$\therefore \Delta = -55$

4)

(1)  $5m^2 = 22m + 15$

$\therefore 5m^2 - 22m - 15 = 0$

$\therefore 5m^2 - 25m + 3m - 15 = 0$

$\therefore 5m(m - 5) + 3(m - 5) = 0$

$\therefore (m - 5)(5m + 3) = 0$

$$\therefore m - 5 = 0 \text{ or } 5m + 3 = 0$$

$$\therefore m = 5 \text{ or } 5m = -3$$

$$\therefore m = 5 \text{ or } m = -\frac{3}{5}$$

$\therefore$  The roots of the given quadratic equation are 5 and  $-\frac{3}{5}$ .

$$(2) \sqrt{3}x^2 + \sqrt{2}x - 2\sqrt{3} = 0$$

Comparing with  $ax^2 + bx + c = 0$  we get,

$$a = \sqrt{3}, b = \sqrt{2}, c = -2\sqrt{3}$$

$$\Delta = b^2 - 4ac$$

$$= (\sqrt{2})^2 - 4 \times \sqrt{3} \times -2\sqrt{3}$$

$$= 2 + 24$$

$$\therefore \Delta = 26$$

As  $\Delta > 0$ , the roots of the quadratic equation are real and unequal.

5)

(1) Let the bigger number be  $x$ .

Now the difference between squares of two number is 120.

$$\therefore x - \text{square of smaller number} = 120$$

$$\therefore \text{square of smaller number} = x - 120$$

According to given condition

$$x - 120 = 2x$$

$$\therefore x - 2x - 120 = 0$$

$$\therefore x - 12x + 10x - 120 = 0$$

$$\therefore x(x - 12) + 10(x - 12) = 0$$

$$\therefore (x - 12)(x + 10) = 0$$

$$\therefore x - 12 = 0 \text{ or } x + 10 = 0$$

$$\therefore x = 12 \text{ or } x = -10$$

$x \neq -10$  as  $x$  is a bigger number.

$$\therefore x = 12$$

Now, square of smaller number =  $x - 120$

$$= (12) - 120$$

$$= 144 - 120$$

$$= 24$$

$$\therefore \text{Smaller number} = \sqrt{24}$$

$$= \sqrt{4} \times 6$$

$$= 2\sqrt{6}$$

$\therefore$  The required number are 12 and  $2\sqrt{6}$ .

$$(2) y^2 - 2y - 7 = 0$$

Comparing with  $ay^2 + by + c = 0$  ...[Here  $y = x$ ] we get,

$$a = 1, b = -2, c = -7$$

$$\therefore \alpha + \beta = \frac{-b}{a} = \frac{-(-2)}{1} = 2 \text{ and}$$

$$\alpha \beta = \frac{c}{a} = \frac{-7}{1} = -7$$

$$(1) \alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$$

$$= (2)^2 - 2 \times (-7)$$

$$= 4 + 14$$

$$= 2$$

$\therefore$

$$\alpha^2 + \beta^2 = 18$$

$$\begin{aligned}(2) \alpha^3 + \beta^3 &= (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta) \\ &= (2)^3 - 3 \times (-7) \times 2 \\ &= 8 + 42 \\ &= 50\end{aligned}$$

$$\therefore \alpha^3 + \beta^3 = 50$$

All the Best

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